Mezinárodní centrum pro informaci a neurčitost

Registrační číslo: CZ.1.07/2.3.00/20.0060



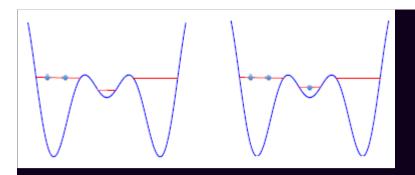


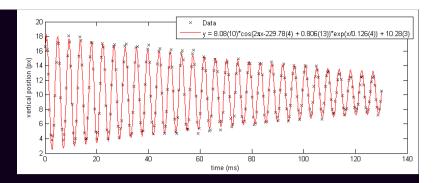




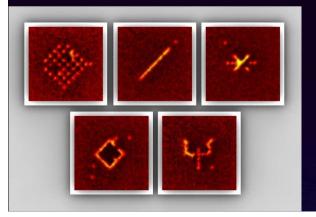
INVESTICE DO ROZVOJE VZDĚLÁVÁNÍ

Tento projekt je spolufinancován Evropským sociálním fondem a státním rozpočtem České republiky.





Resources for quantum technologies



Jacob Sherson

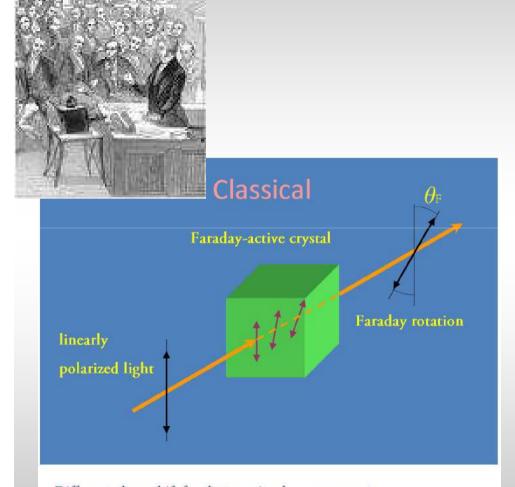
Olomouc 26/6-2012



Outline

- Non-destructive imaging
 - Triple-well atomtronics
 - The quantum computer game

Faraday rotation (1845)

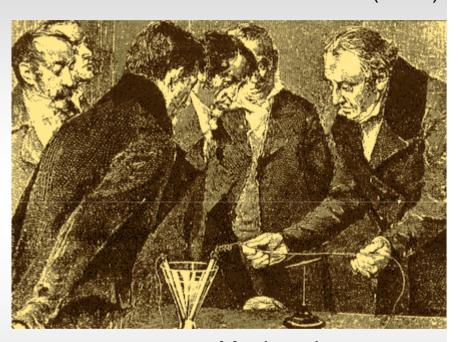


Different phase shift for the two circular components:

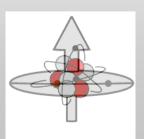
- Jones vector notation

$$\begin{pmatrix} 1 \\ 0 \end{pmatrix} = \frac{1}{2} \begin{bmatrix} 1 \\ -i \end{pmatrix} + \begin{pmatrix} 1 \\ i \end{bmatrix} \rightarrow \frac{1}{2} \begin{bmatrix} e^{i\theta_F} \begin{pmatrix} 1 \\ -i \end{pmatrix} + e^{-i\theta_F} \begin{pmatrix} 1 \\ i \end{pmatrix} \end{bmatrix} = \begin{pmatrix} \cos \theta_F \\ \sin \theta_F \end{pmatrix}$$

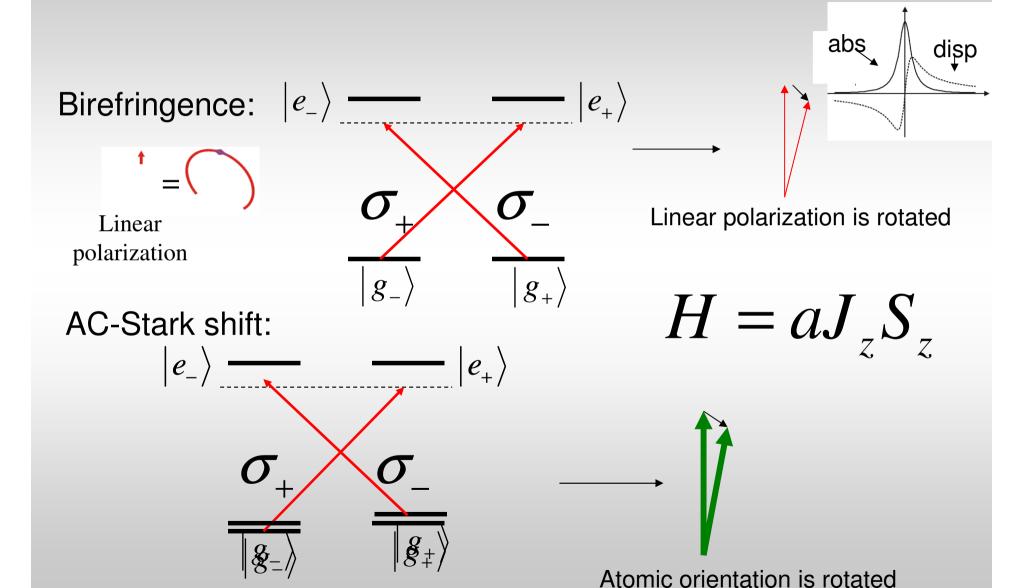
H. C. Ørsted (1820)



Moving charges generate magnetic fields.

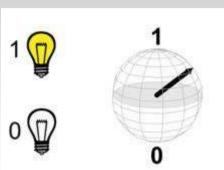


Faraday rotation, quantum version



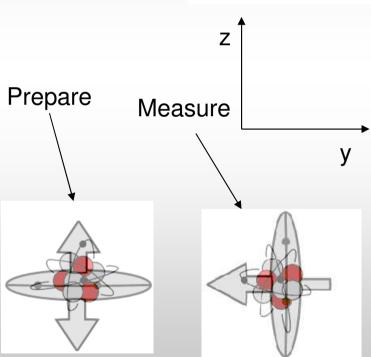
Complementarity

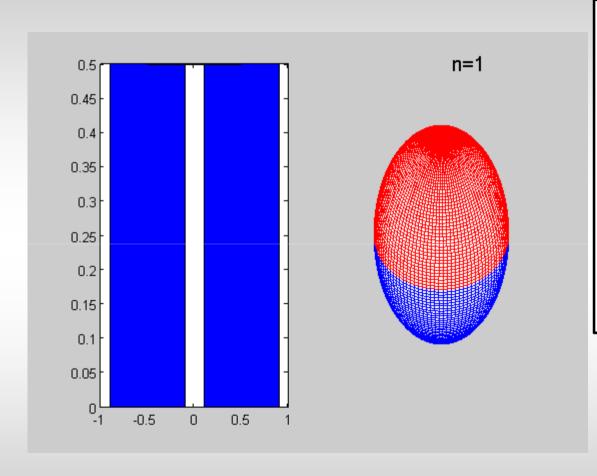
Single atom: 2 possible spins in each direction



If two quantities are complementary, they cannot be known precisely at the same time

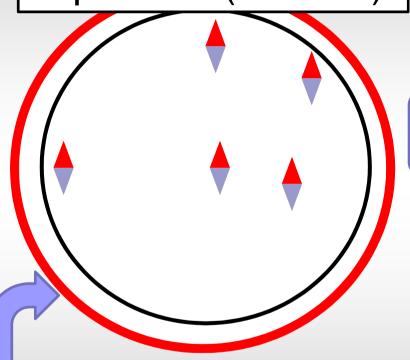






- Relative size of quantum fluctuations decreases
- discrete -> Continuous variables

Room temperature vapor cell (N~10¹²)







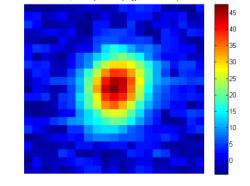
Nature 2004: Experimental demonstration of quantum memory for light

Nature 2006: Quantum teleportation between light and matter

Ultracold cloud (N~10⁵)

Two options:

- Longitudinal probing (classical)
- Transverse probing (quantum)



2012\week#7\2012-02-15\158 single picture\loadTifFaradavHistogram quick.m

Århus experiment

Research group members:



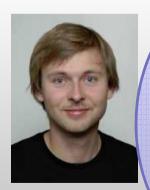
Jan Arlt Associate Prof

Miroslav Gajdacz



Jacob Sherson
Assistant Prof

Ultracold Bosons in Optical Lattises



Poul Pedersen

Multi Species Quantum Gases



Nils Winter



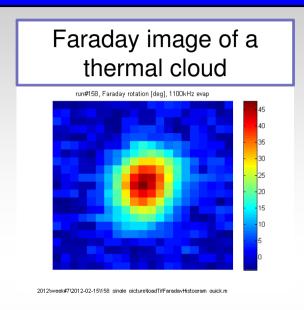
Lars Wacker

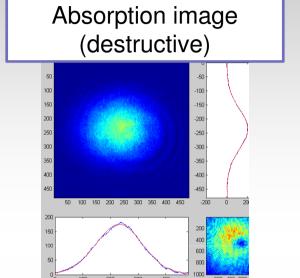
High resolution lab



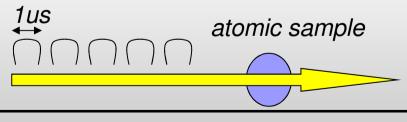
Romain Müller

Non-destructive imaging and feedback



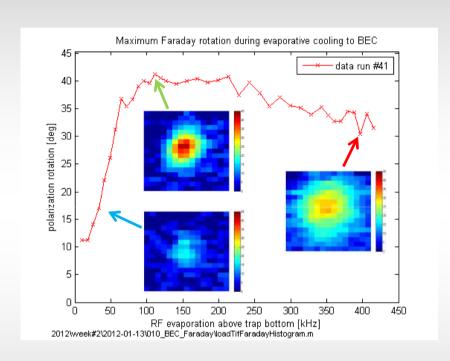


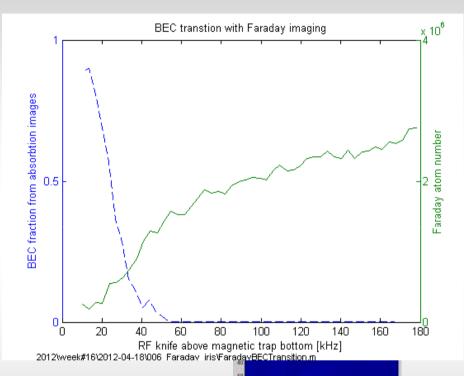
Absorption probability 0.003 per pulse!



Continuous measurements

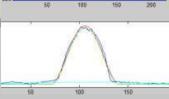
Single run monitoring of BEC transition





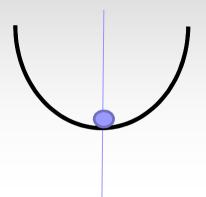
- multiple non-destructive pictures during cooling sequence
- sudden drop of maximum Faraday angle

BEC confirmed by absorption image at the en-



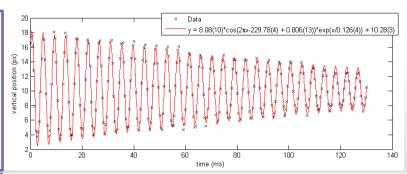
Non-destructive imaging and feedback

Suddenly shift the position of the trap

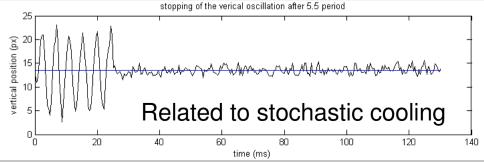


- Fast characterization of trap parameters
- Possibility for quantum (feedback) control

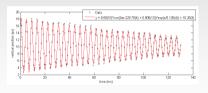
300 images of the same oscillating cloud



Stopping the motion of an oscillating cloud



Some future perspectives

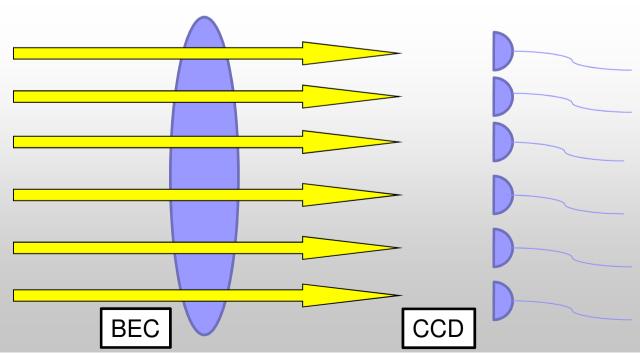


Measure and influence fundamental excitation modes of a BEC

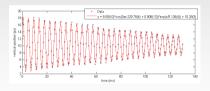
- Squeezing
- Entanglement
- Fock- and Schrödinger cat states

12

Bogoluibov modes

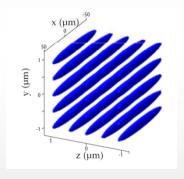


Some future perspectives



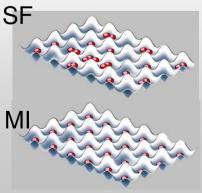
Measure and influence fundamental excitation modes of a BEC

- Squeezing
- Entanglement
- Fock- and Schrödinger cat states



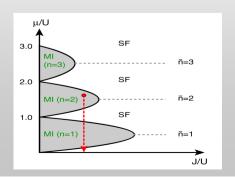
QND probing of a single 1D tube in a 2D optical lattice

- High capacity quantum memory
- Large Schrödinger cat states



QND probing of interacting quantum many-body states

Modify quantum phase diagrams



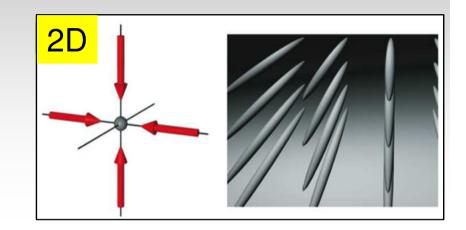
Outline

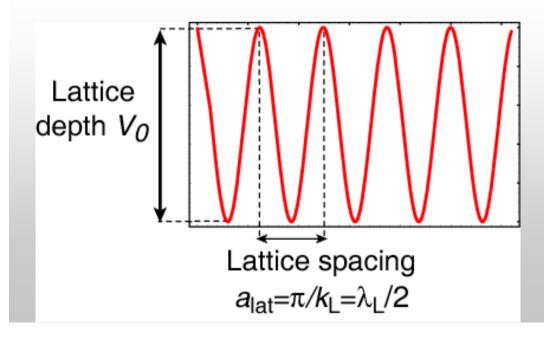
- Non-destructive imaging
- Triple-well atomtronics
 - The quantum computer game

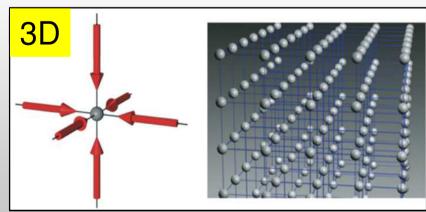
Optical lattices



Potential: $V(x) = V_0 \sin^2(k_{\rm L} x)$





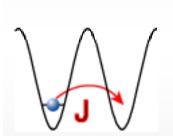


Bose-Hubbard Hamiltonian

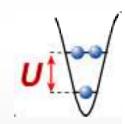
Expanding the field operator in the Wannier basis of localized wave functions on each lattice site, yields:

$$\hat{\psi}(\mathbf{x}) = \sum_{i} \hat{a}_{i} w(\mathbf{x} - \mathbf{x}_{i})$$

Bose-Hubbard Hamiltonian



$$H = -J\sum_{\langle i,j\rangle} \hat{a}_i^{\dagger} \hat{a}_j + \sum_i \varepsilon_i \hat{n}_i + \frac{1}{2} U \sum_i \hat{n}_i (\hat{n}_i - 1)$$



Tunnelmatrix element/Hopping element

$$J = -\int d^3x \, w(\mathbf{x} - \mathbf{x}_i) \left(-\frac{\hbar^2}{2m} \nabla^2 + V_{lat}(\mathbf{x}) \right) w(\mathbf{x} - \mathbf{x}_j)$$

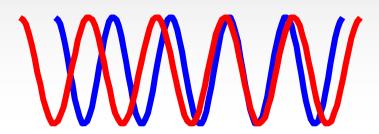
Onsite interaction matrix element

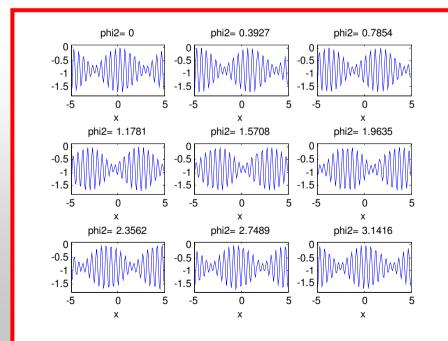
$$U = \frac{4\pi \hbar^2 a}{m} \int d^3 x \left| w(\mathbf{x}) \right|^4$$

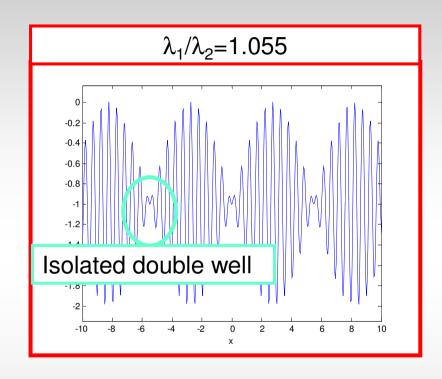
M.P.A. Fisher et al., PRB 40, 546 (1989); D. Jaksch et al., PRL 81, 3108 (1998)

Large period superlattice

Overlap two standing waves of close lying frequency







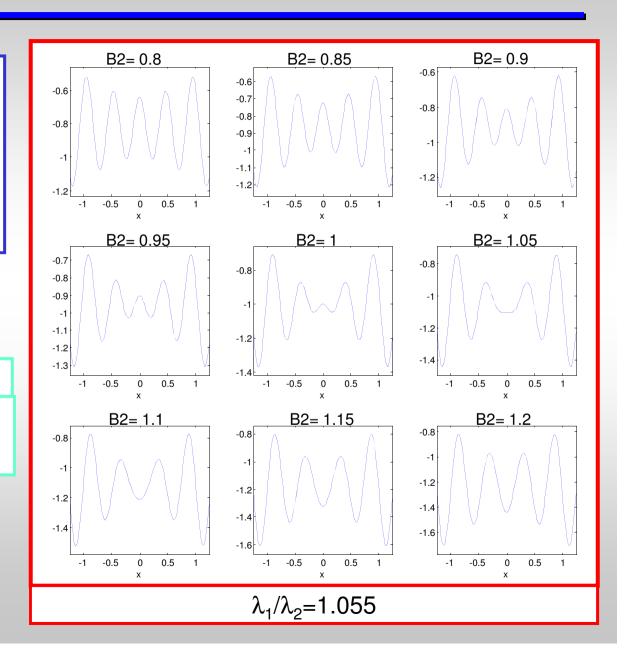
Scanning the relative phase using frequency adjustment allows for ultra-precise addressing of individual sites

Double well dynamics

- The relative amplitude gives full control of the barrier height
- The relative phase controls the asymmetry of the double well

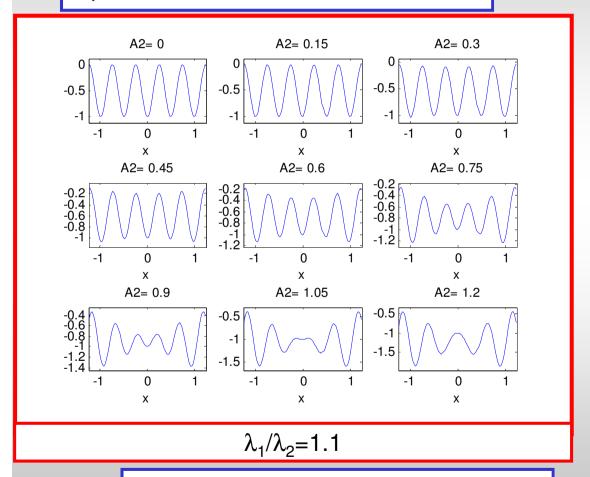
Perspectives

- Local double well merger
- Local directed transport

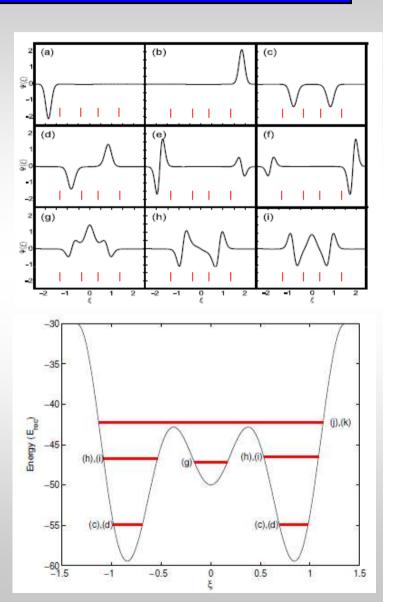


Triple well dynamics: towards atomtronics

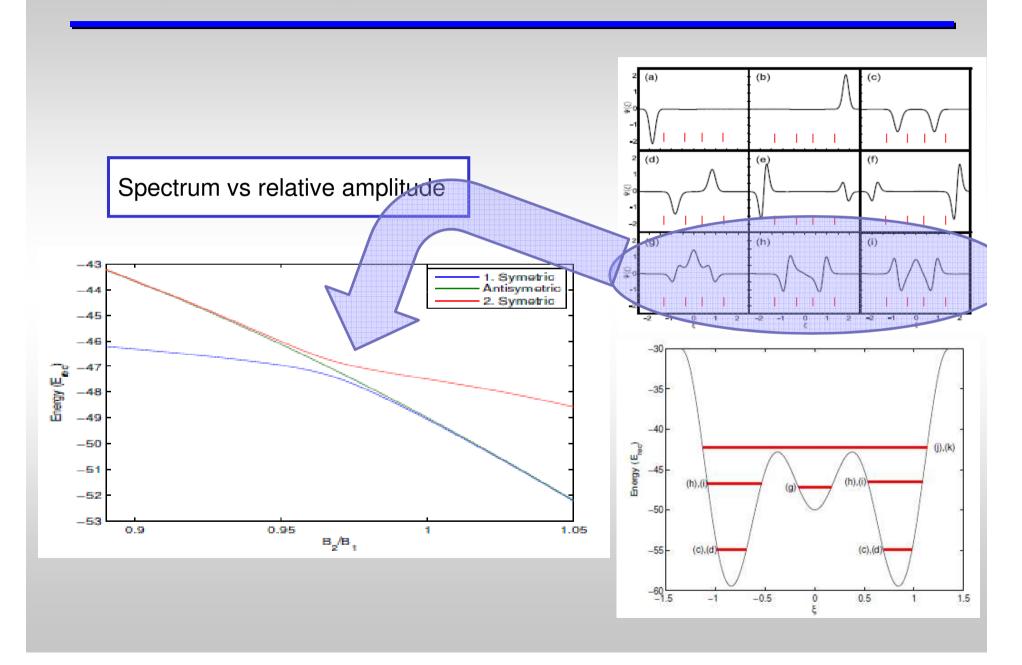
Different choice of relative phase: triple well



Adjusting the relative amplitude gives full control of the middle well depth

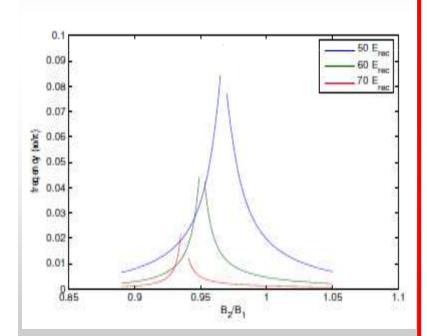


Triple well dynamics: towards atomtronics

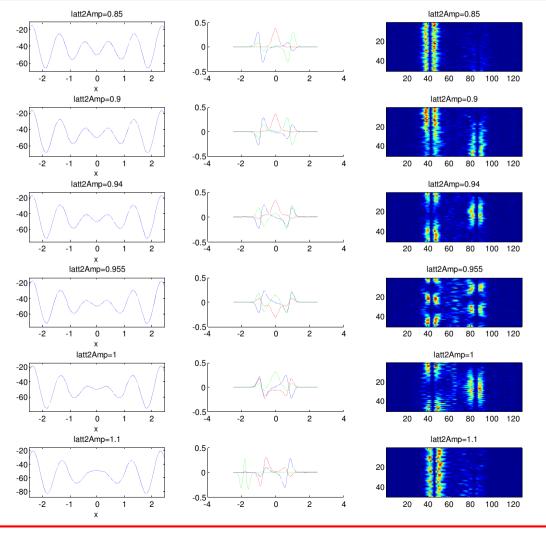


Triple well dynamics

- Place an atom in the 1st excited state of the left well (200 Erec)
- Quench to 50 Erec
- Evolve in time



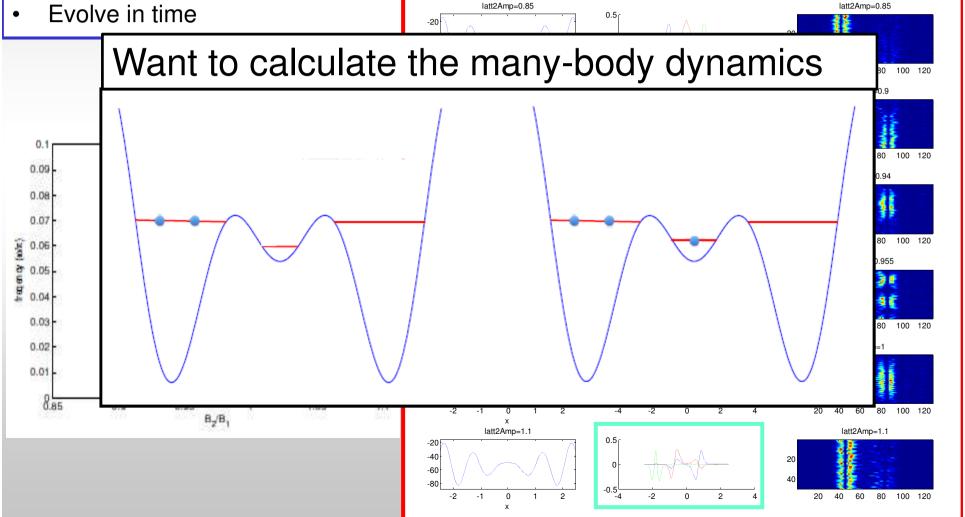
Transistor like tunneling behavior



Triple well dynamics

- Place an atom in the 1st excited state of the left well (200 Erec)
- Quench to 50 Erec
- Evolve in time

Transistor like tunneling behavior



Creating localized initial states

Calculate overlap with eigenstates

$$p_{\mathrm{L},i} = \langle \Phi_i | \psi_{\mathrm{L}} \rangle$$
$$p_{\mathrm{R},i} = \langle \Phi_i | \psi_{\mathrm{R}} \rangle$$

Define "localized states"

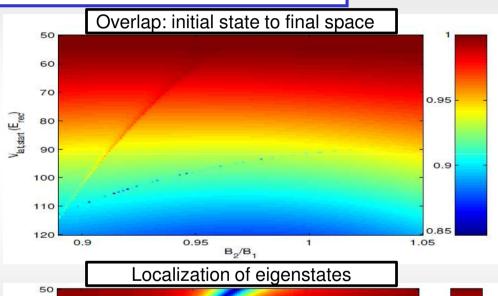
$$\Psi_{L} = \sum_{i \in \{a, s, g\}} p_{L,i} \Phi_{i}$$

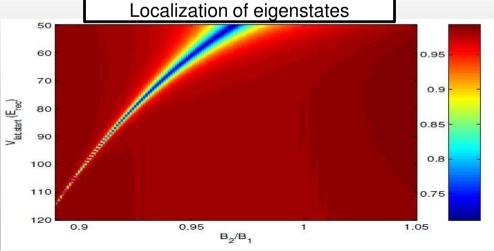
$$\Psi_{\mathbf{R}} = \sum_{i \in \{\mathbf{a}, \mathbf{s}, \mathbf{g}\}} p_{\mathbf{R}, i} \Phi_{i}$$

$$\mathbf{p}_{\mathrm{M}} = \mathbf{p}_{\mathrm{L}} \times \mathbf{p}_{\mathrm{L}}$$

$$\Psi_{\mathbf{M}} = \sum_{i \in \{\mathbf{a}, \mathbf{s}, \mathbf{g}\}} \mathbf{p}_{\mathbf{M}, i} \Phi_{i}$$

- Place an atom in the 1st excited state of the left well (120-50 Erec)
- Quench to 50 Erec





Creating localized initial states

Calculate overlap with eigenstates

$$p_{\mathrm{L},i} = \langle \Phi_i | \psi_{\mathrm{L}} \rangle$$
$$p_{\mathrm{R},i} = \langle \Phi_i | \psi_{\mathrm{R}} \rangle$$

Define "localized states"

$$\Psi_{L} = \sum_{i \in \{a, s, g\}} p_{L,i} \Phi_{i}$$

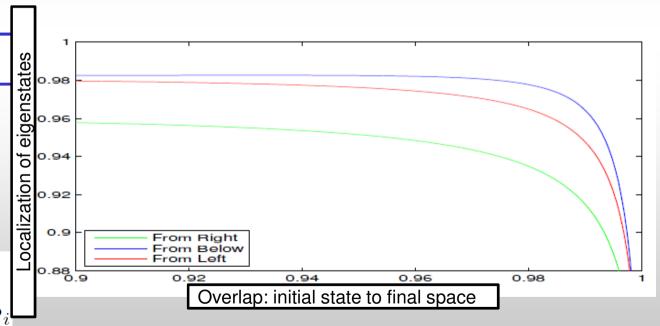
$$\Psi_{R} = \sum_{i \in \{a, s, g\}} p_{R,i} \Phi_{i}$$

$$\mathbf{p}_{M} = \mathbf{p}_{L} \times \mathbf{p}_{L}$$

$$\Psi_{M} = \sum_{i \in \{a, s, g\}} \mathbf{p}_{M,i} \Phi_{i}$$

- Projection from deep lattice (below)
- Projection from lattice 1 highest power (left)
- Projection from lattice 2 highest power (right)

$$B_2/B_1 = 0.969$$



Define Fock states

$$|n_1, n_2, n_3\rangle = \left(\prod_{i \in \{1, 2, 3\}} \frac{1}{\sqrt{n_i!}} (\hat{a}_i^{\dagger})^{n_i}\right) |0, 0, 0\rangle$$

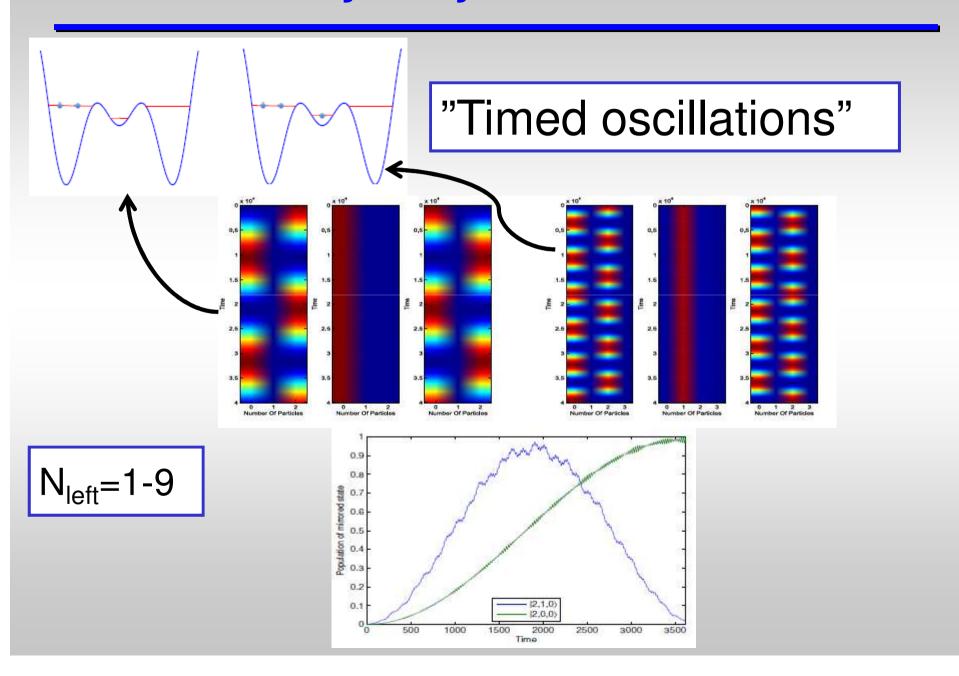
Bose-Hubbard Hamiltonian

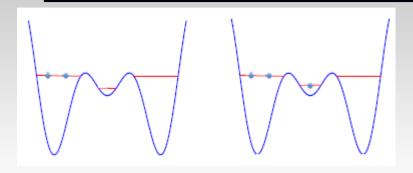
$$H = -\sum_{\langle i,j\rangle} J_{i,j} \hat{a}_i^{\dagger} \hat{a}_j + \frac{1}{2} \sum_i U_{i,i} \hat{n}_i (\hat{n}_i - 1)$$
$$+ \frac{1}{2} \sum_i \sum_j U_{i,j} \hat{n}_i \hat{n}_j + \sum_i \epsilon_i \hat{n}_i,$$

nxn matrix

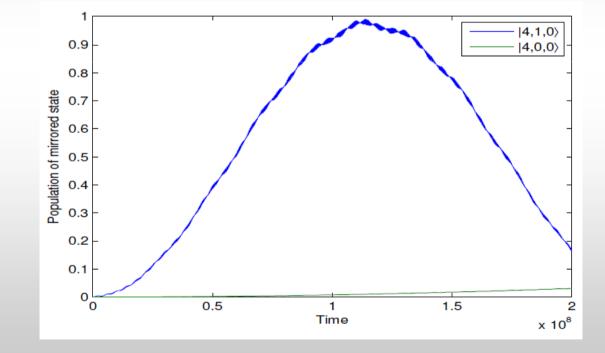
$$H_{i,j} = \langle F_i | H_{\rm BH} | F_j \rangle$$

Evolve according to
$$|\Psi(t)\rangle = e^{\frac{iHt}{\hbar}}|\Psi_0\rangle$$

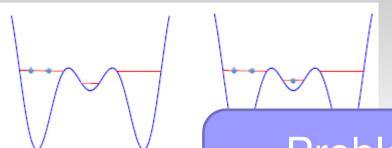




"Blocked oscillations" (high interaction)



 $N_{left}=4$



"Blocked oscillations"

Problem: time scales become very long

N_{left}=4

Solution: single-particle tunneling in a tilted well -> dynamically transfer N atoms

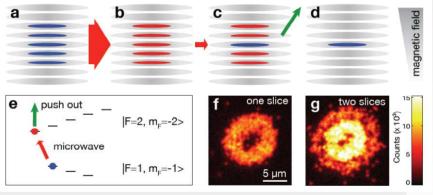


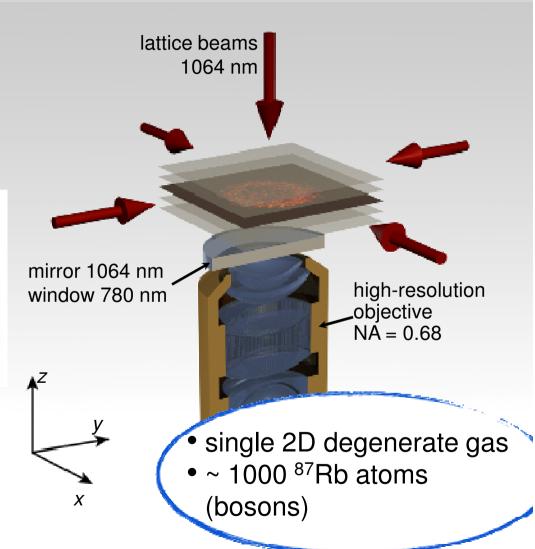
Outline

- Non-destructive imaging
- Triple-well atomtronics
- The quantum computer game

Experimental set-up

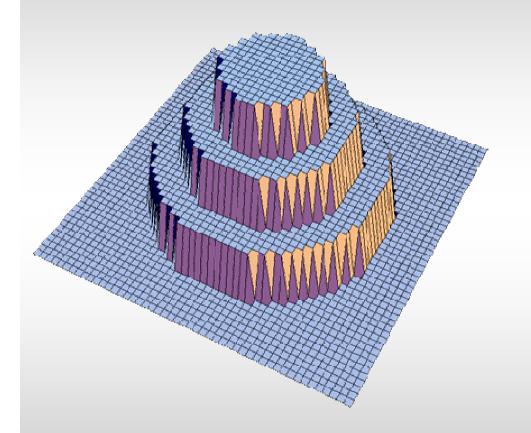
Preparation of a single 2D system:

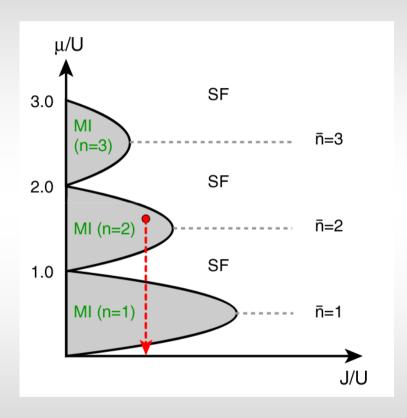




J. F. Sherson et al, **Nature**, **467**, 68 (2010)

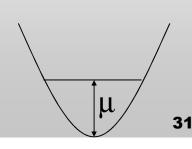
Superfluid – Mott-Insulator Phase Diagram



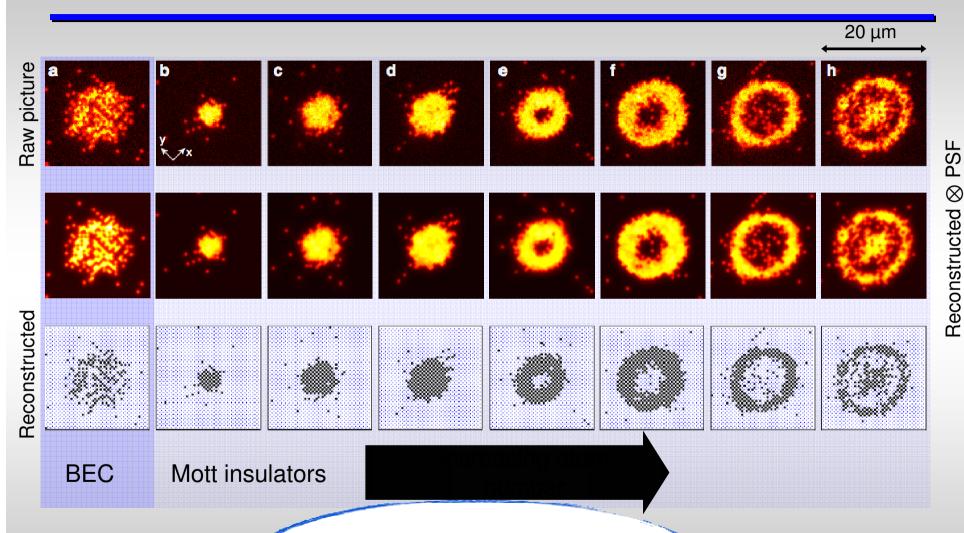


Inhomogeneous system: effective local chemical potential

$$\mu_{loc} = \mu - \varepsilon_i$$



In-situ observation of a Mott insulator



for the Mott insulators: U/J ~ 300 (critical U/J ~16)

> only thermal fluctuations

J. F. Sherson et al, **Nature**, **467**, 68 (2010)

Detection of many-body physics

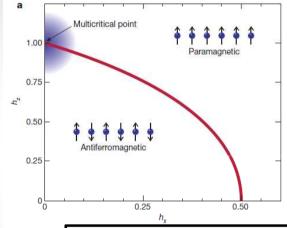
Quantum simulation of antiferromagnetic spin chains in an optical lattice

Jonathan Simon¹, Waseem S. Bakr¹, Ruichao Ma¹, M. Eric Tai¹, Philipp M. Preiss¹ & Markus Greiner¹

21 APRIL 2011 | VOL 472 | NATURE | 307

1D Ising chain

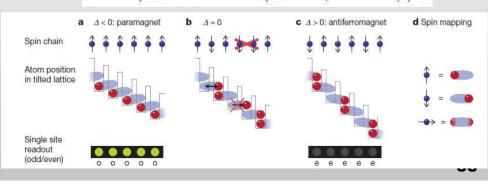
$$H = J \sum_{i} S_{z}^{i} S_{z}^{i+1} - h_{z}^{i} S_{z}^{i} - h_{x}^{i} S_{x}^{i}$$
Multicritical point
$$A A A A A A$$



Tilted optical lattice

$$(h_z, h_x) = (1 - \tilde{\Delta}, 2^{3/2} \tilde{t})$$

$$= t/J, \quad \tilde{\Delta} = \Delta/J = (E - U)/J$$



Detection of many-body physics

Quantum simulation of antiferromagnetic spin chains in an optical lattice

Jonathan Simon¹, Waseem S. Bakr¹, Ruichao Ma¹, M. Eric Tai¹, Philipp M. Preiss¹ & Markus Greiner¹

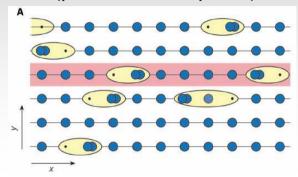
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Observation of Correlated Particle-Hole Pairs and String Order in Low-Dimensional Mott Insulators

M. Endres, ¹* M. Cheneau, ¹ T. Fukuhara, ¹ C. Weitenberg, ¹ P. Schauß, ¹ C. Gross, ¹ L. Mazza, ¹ M. C. Bañuls, ¹ L. Pollet, ² I. Bloch, ^{1,3} S. Kuhr^{1,4}

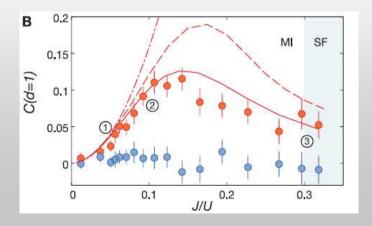
14 OCTOBER 2011 VOL 334 SCIENCE

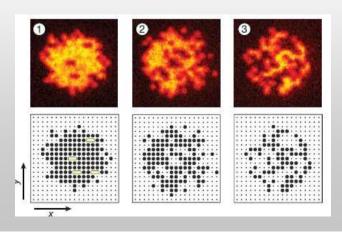
1D tunneling close to MI transition (particle-hole pairs)



Two-site parity correlation function

$$C(d) = \langle \hat{s}_k \hat{s}_{k+d} \rangle - \langle \hat{s}_k \rangle \langle \hat{s}_{k+d} \rangle$$
$$\hat{s}_k = e^{i\pi \delta \hat{n}_k}$$





Detection of many-body physics

Quantum simulation of antiferromagnetic spin chains in an optical lattice

Jonathan Simon¹, Waseem S. Bakr¹, Ruichao Ma¹, M. Eric Tai¹, Philipp M. Preiss¹ & Markus Greiner¹

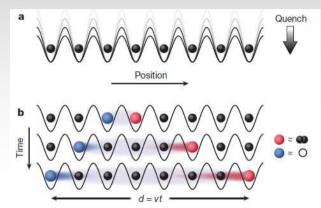
21 APRIL 2011 | VOL 472 | NATURE | 307

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14 OCTOBER 2011 VOL 334 SCIENCE

Quench from U/J=40 to U/J=9



Two-site parity correlation function

$$C(d) = \langle \hat{s}_k \hat{s}_{k+d} \rangle - \langle \hat{s}_k \rangle \langle \hat{s}_{k+d} \rangle$$
$$\hat{s}_k = e^{i\pi \delta \hat{n}_k}$$

O and a second s

Light-cone-like spreading of correlations in a quantum many-body system

Marc Cheneau¹, Peter Barmettler², Dario Poletti², Manuel Endres¹, Peter Schauß¹, Takeshi Fukuhara¹, Christian Gross¹, Immanuel Bloch^{1,3}. Corinna Kollath^{2,4} & Stefan Kuhr^{1,5}

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Global manipulation

The 'Higgs' Amplitude Mode at the Two-Dimensional Superfluid-Mott Insulator Transition

Manuel Endres^{1,*}, Takeshi Fukuhara¹, David Pekker², Marc Cheneau¹, Peter Schauβ¹, Christian Gross¹, Eugene Demler³, Stefan Kuhr⁴, and Immanuel Bloch^{1,5}

arXiv:1204.5183v2 [cond-mat.quant-gas] 25 Apr 2012

SF-MI phase transition has a complex order parameter

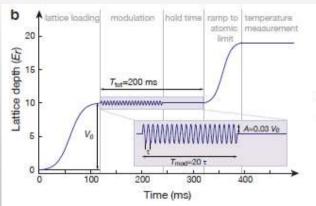
$$\Psi = |\Psi|e^i$$

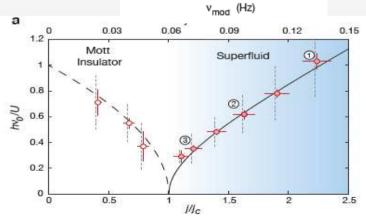
Spontaneous symmetry breaking in the SF phase

Nambu-Geldstone Mode Re(Ψ)

Ni_o≥1

Ni_o≥1 Using weak amplitude modulation detect a gap in the response





0 200 400 600 800 1000

0.18

0.18

0.16

 $V_0=8E_r$ $j/j_c=2.2$

V0=9Er j/j_c=1.6

 $V_0=10E_r$

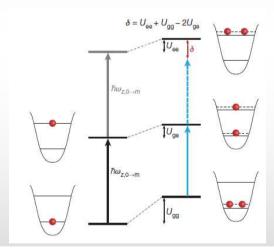
 $j/j_{c}=1.2$

Global manipulation

Orbital excitation blockade and algorithmic cooling in quantum gases

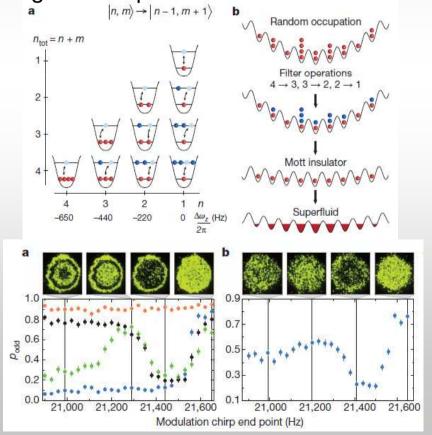
Waseem S, Bakr1, Ph 500 | NATURE | VOL 480 | 22/29 DECEMBER 2011 ier1

Two-particle interaction energy depends on the vibrational state



$$U_{\nu,\mu} = U_{00} \begin{pmatrix} 1 & 1 & 0.75 & \dots \\ 1 & 0.75 & 0.875 & \dots \\ 0.75 & 0.875 & 0.64 & \dots \\ \vdots & \vdots & \vdots & \ddots \end{pmatrix}$$

Filtering: sequentially excite and remove higher occupational numbers



Global manipulation

Orbital excitation blockade and algorithmic cooling in quantum gases

Waseem S, Bakr1, Ph 500 | NATURE | VOL 480 | 22/29 DECEMBER 2011 ier1

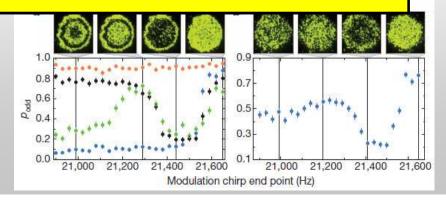
Two-particle interaction energy depends on the vibrational state

Filtering: sequentially excite and remove higher occupational numbers

Random occupation

- Entropy per particle is reduced dramatically in the center but not globally
- Vacancies are not removed

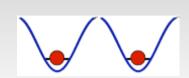
$$U_{\nu,\mu} = U_{00} \begin{pmatrix} 1 & 1 & 0.75 & \dots \\ 1 & 0.75 & 0.875 & \dots \\ 0.75 & 0.875 & 0.64 & \dots \\ \vdots & \vdots & \vdots & \ddots \end{pmatrix}$$



Shaking the entropy out of an optical lattice: removing vacancies

Would like to realize an "OR" operation between 2 sites

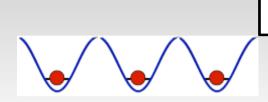
Forbidden due to unitarity



Vacancy probability: ε

Shaking the entropy out of an optical lattice: removing vacancies

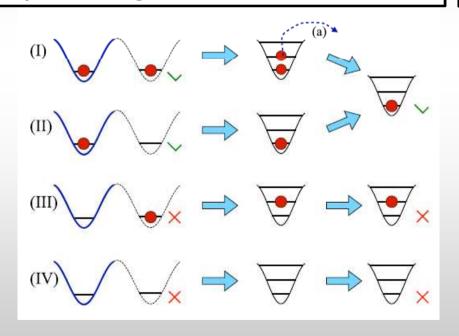
Need 3 sites: Target well + 2 aux wells

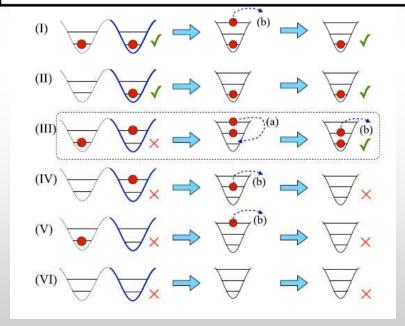


Vacancy probability: ε

Step 1: merge middle and left well

Step 2: merge middle and right well

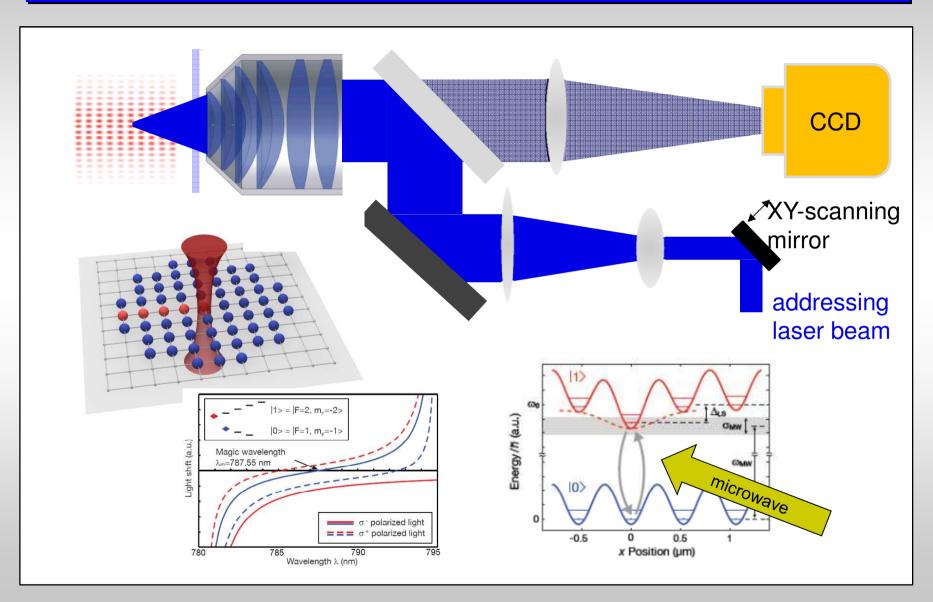




Final vacancy probability: $2\varepsilon^2 - \varepsilon^3$

Malte Tichy, Klaus Mølmer, and JFS, arxiv:1012.1457v2 (2010)

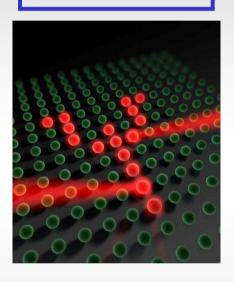
Addressing individual lattice sites

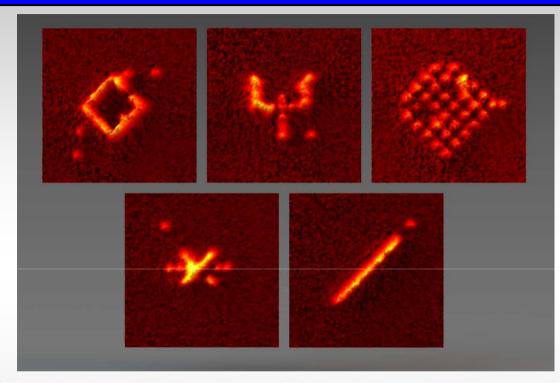


Weitenberg et al, **Nature**, **471**, 319 (2011)

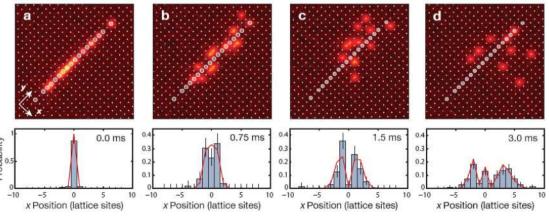
Addressing individual lattice sites

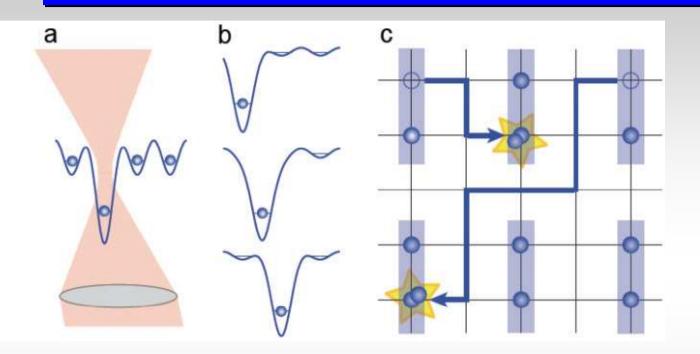
Writing arbitrary patterns





Single particle tunneling "the horse track race"





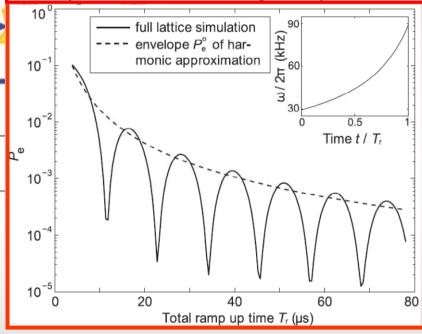
- a)Ramp up tweezer
- b) Transport atom by translating tweezer
- c)Collisional gate by merging atoms

a)Ramp up tweezer

Increase trap frequency according to the adiabaticity criterion:

$$\hbar \left| \frac{\mathrm{d}\omega(t)}{\mathrm{d}t} \right| = \xi \frac{(\Delta E_{ge})^2}{\left| \langle \phi_e | \frac{\partial H}{\partial \omega} | \phi_g \rangle \right|}$$

Numerical solution of the timedependent Schrödinger equation



Solve analytically in a two-state harmonic oscillator model

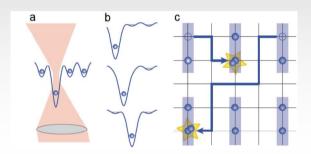
$$P_{\rm e}^{\rm harm}(t) = P_{\rm e}^0 \sin^2 \left[\frac{\sqrt{2\xi^2 + \frac{1}{2}} \log[1 - 4\sqrt{2}t\xi\omega_o]}{4\xi} \right]$$

With envelope:

$$P_e^0 = 4\xi^2/(1+4\xi^2)$$

C. Zhang, V. W. Scarola, and S. Das Sarma, Phys. Rev. A 75, 060301(R) (2007).

b)Transport atom



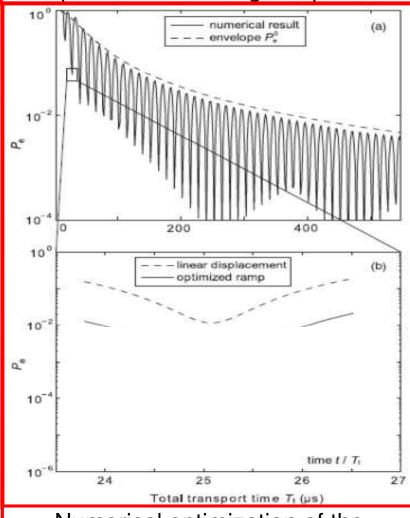
Shift tweezer position (linearly) according to the adiabaticity criterion:

$$\hbar \left| \frac{\mathrm{dx}_{o}(t)}{\mathrm{dt}} \right| = \xi \frac{(\Delta E_{ge})^{2}}{\left| \langle \phi_{e} | \frac{\partial H}{\partial x_{o}} | \phi_{g} \rangle \right|}$$

Solve analytically in a two-state harmonic oscillator model

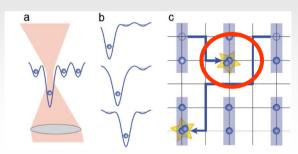
$$P_{\rm e}^{\rm harm}(t) = P_{\rm e}^0 \sin^2[\sqrt{1 + 4\xi^2}\omega t/2]$$

With envelope: $P_e^0 = 4\xi^2/(1 + 4\xi^2)$ Weitenberg et al, PRA (2011) Numerical solution of the timedependent Schrödinger equation



Numerical optimization of the translation profile

c)2-qubit exchange gate



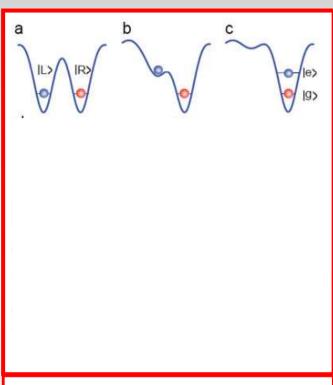
- Map left well atom to first excited state of the right well
- The atom is now in a superposition of the singlet and triplet combinations

$$|s\rangle = |\uparrow\rangle_{g}|\downarrow\rangle_{e} - |\downarrow\rangle_{g}|\uparrow\rangle_{e},$$

$$|t_{0}\rangle = |\uparrow\rangle_{g}|\downarrow\rangle_{e} + |\downarrow\rangle_{g}|\uparrow\rangle_{e},$$

$$|t_{-1}\rangle = |\downarrow\rangle_{g}|\downarrow\rangle_{e},$$

$$|t_{+1}\rangle = |\uparrow\rangle_{g}|\uparrow\rangle_{e}.$$



99.97% fidelity in 75 us

Interactions in the triplet state drive oscillations

$$\Psi(t = 0) = |s\rangle + |t_0\rangle \sim |\uparrow\rangle_g|\downarrow\rangle_e,$$

$$\Psi(t) = |s\rangle + e^{iU_{eg}t/\hbar}|t_0\rangle,$$

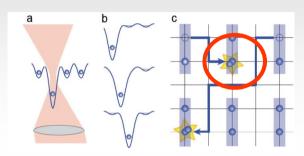
$$\Psi(t = T_{\text{swap}}) = |s\rangle - |t_0\rangle \sim |\downarrow\rangle_g|\uparrow\rangle_e,$$

$$\Psi(t = T_{\text{swap}}/2) = |s\rangle + i|t_0\rangle \sim |\uparrow\rangle_g|\downarrow\rangle_e + i|\downarrow\rangle_g|\uparrow\rangle_e.$$

$$\sqrt{\text{SWap gate}}$$

Weitenberg et al, PRA (2011)

c)2-qubit exchange gate



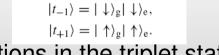
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$$|t_{-1}\rangle = |\downarrow\rangle_{g}|\downarrow\rangle_{e},$$

$$|t_{+1}\rangle = |\uparrow\rangle_{g}|\uparrow\rangle_{e}.$$



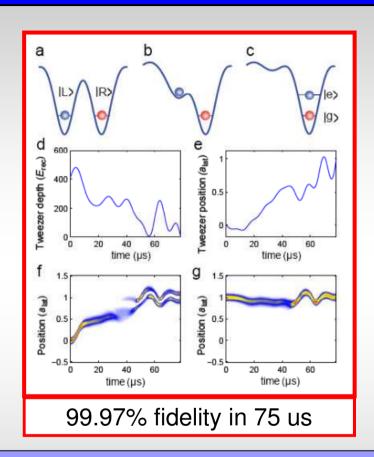
Interactions in the triplet state

$$\Psi(t=0) = |s\rangle + |t_0\rangle \sim |\uparrow\rangle_g |\downarrow\rangle_e,$$

$$\Psi(t) = |s\rangle + e^{iU_{eg}t/\hbar} |t_0\rangle,$$

$$\Psi(t=T_{\text{swap}}) = |s\rangle - |t_0\rangle \sim |\downarrow\rangle_g |\uparrow\rangle$$

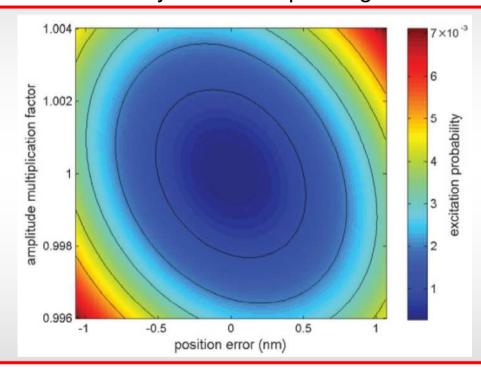
$$\Psi(t=T_{\text{swap}}/2) = |s\rangle + i|t_0\rangle \sim |\uparrow\rangle_g |\downarrow\rangle_e + i$$



Total gate time a few 100us with 10⁻³ error

Weitenberg et al, PRA (2011)

Include intensity and beam pointing instabilities



Three solutions:

- Improve state-of-the-art a la LIGO
- The quantum computer game
- A fundamentally new method for addressing

Current state-of-the-art of 50nm beam pointing accuracy yields considerably higher errors!

Human Computing

9 billion man-hours spent on solitaire per year!



ESP game: 22,000 players Over 3,2 mio image-labels



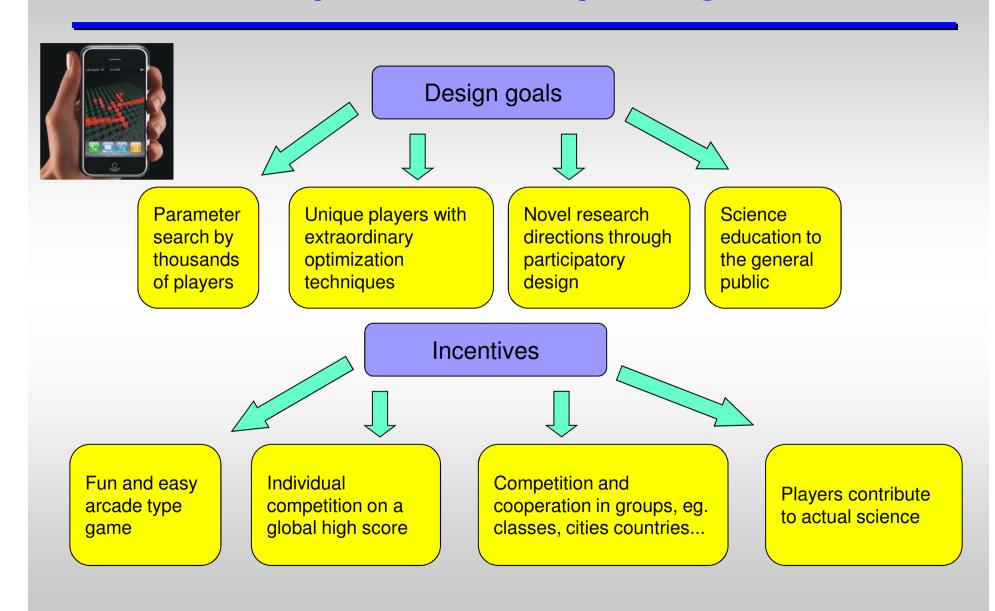
Human Computing

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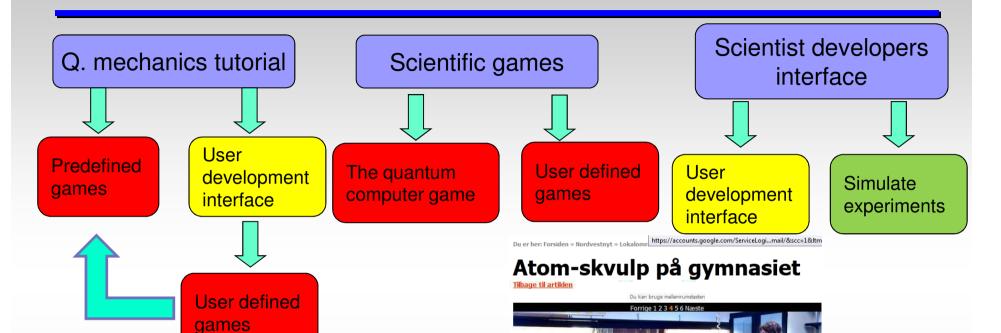


- >100.000 players
- Players invent new algorithms (15 year super-player)
- Players helped the scientists win the CASP 2009 protein folding challenge

The quantum computer game

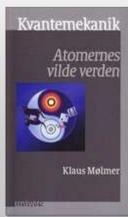


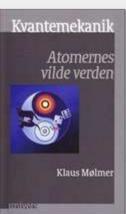
Quantum games: software overview



High school / university projects:

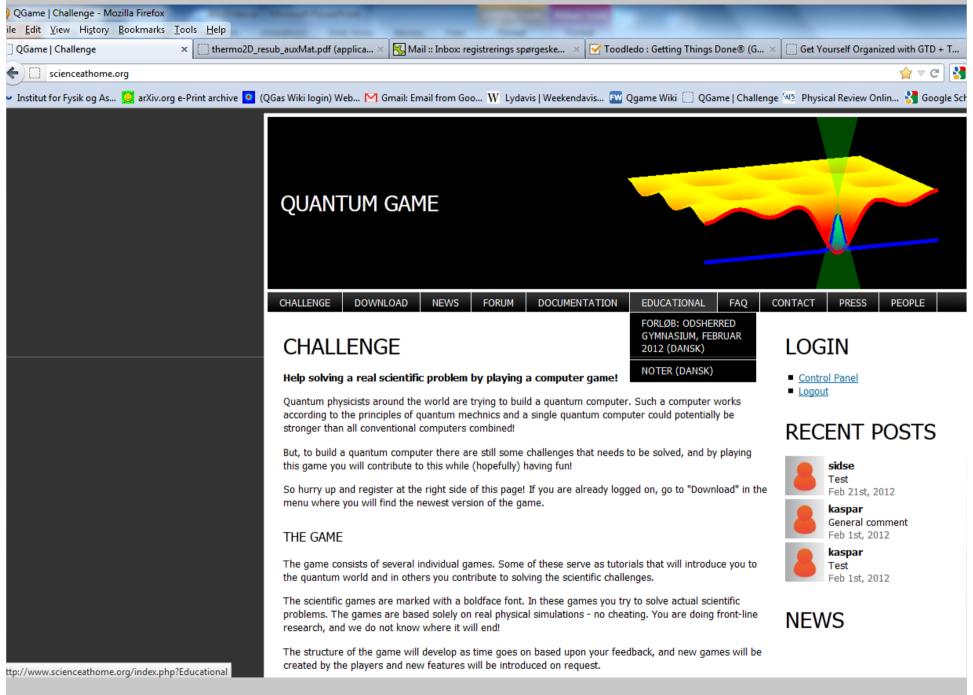
- 1-2 week course
- Combined with q. mechanics book of Klaus Mølmer





.∍s available (TDSE) vskii ard

Feb 2012: first successful high-school project



Classical example: Harmonic motion

Move the wall according to $x_o(t)$

 $x_{o}(t)$

x(t)

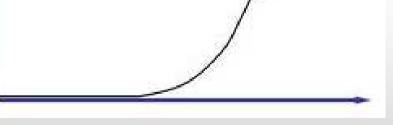


Newtons 2nd lov:

$$F = m \ddot{x} = -k (x(t) - x_o(t))$$

Exercise: the mass has to move according to:

$$x(t) = \frac{1}{1 + e^{-t}}$$



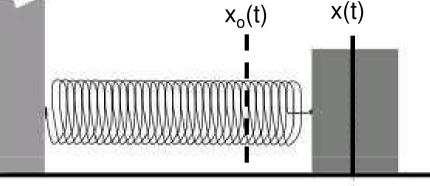
Classical example: Harmonic motion

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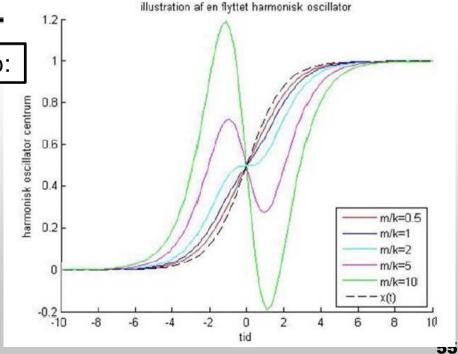


Exercise: the mass has to move according to:

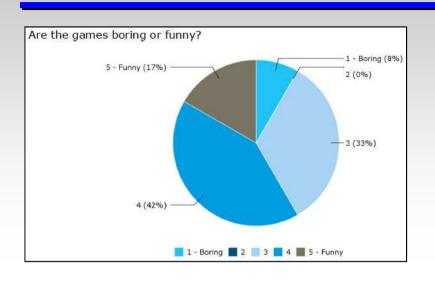
$$x(t) = \frac{1}{1 + e^{-t}}$$

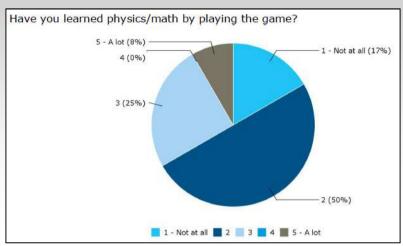
What should $x_o(t)$ be?

$$x_o(t) = x(t) + \frac{m}{k} \ddot{x}$$



Evaluation results





"Especially competitive aspect of the game is a scoop. It's almost like taking advantage of the most primal part of humans to explore science."

"Quantum physics seems suddenly more tangible, something which is not a dangerous monster you can't work out. It should be in every school!"

"In the normal teaching you calculate it only while you in the game get the feeling of directly doing the experiment"

"I think you have found a super mix of tutorial games and difficult scientific games.

